Transport Properties of 1,1-Difluoroethane (R152a)

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Based on reliable, carefully selected data sets, equations for the thermal conductivity and the viscosity of the refrigerant R 152a are presented. They are valid at temperatures from 240 to 440 K, pressures up to 20 MPa, and densities up to 1050 kg \cdot m⁻³, including the critical region.

KEY WORDS: I,I-difluoroethane; correlation: critical region: HFC-152a: R152a; thermal conductivity: transport properties: viscosity.

1. INTRODUCTION

1,1-Difluoroethane (R152a) is one of the most promising long-term replacement refrigerants for chlorofluorocarbons (CFCs), whose production is to be phased out by 1996 according to the Montréal protocol. R152a combines a zero ozone-depletion potential (ODP) and a comparatively low global-warming potential of 150 (relative to CO , for a 100-year integration time horizon) [1] with other properties desirable for refrigerants such as a low toxicity, chemical stability, and compatibility with lubricant oils, the only disadvantage being its flammability. For this reason it is used as a component of binary or ternary mixtures of HFCs. This application implies a demand for reliable expressions for the transport properties of R152a.

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A preliminary evaluation and correlation of the transport properties, which omitted critical enhancements, was published by two of the present authors [2, 3], However, in practice the thermal conductivity exhibits a pronounced critical enhancement in a large range of temperatures and densities [4, 5]. An equation for the thermodynamic properties of R152a in the critical region has recently been developed by van Pelt and Sengers [6] as a supplement to a global equation for the thermodynamic properties of R152a provided by Tillner-Roth [7]. Hence, it is now possible to present equations for the transport properties of R152a over an appreciable range of temperatures and densities including the critical region.

2. METHODOLOGY

In the present evaluation and correlation of the viscosity and thermal conductivity of R152a we apply the residual concept following the evaluation and correlation scheme outlined in detail in previous publications [8-11]. That is, within the uncertainty of the measurements, the viscosity $n(\rho, T)$ and the thermal conductivity $\lambda(\rho, T)$, respectively, as a function of density ρ and temperature T may be represented as the sum of three contributions:

$$
\eta(\rho, T) = \eta_0(T) + \Delta_R \eta(\rho) + \Delta_c \eta(\rho, T) \tag{1}
$$

$$
\lambda(\rho, T) = \lambda_0(T) + \Delta_R \lambda(\rho) + \Delta_c \lambda(\rho, T) \tag{2}
$$

The dilute-gas contributions $\eta_0(T)$ and $\lambda_0(T)$ depend only on the temperature. They can be treated independently from the other contributions. The excess terms $A_R \eta(\rho)$ and $A_R \lambda(\rho)$ account for the pressure or density dependence in the absence of critical fluctuations. As was the case for R134a [9], we neglect any temperature dependence of the excess terms because the resulting errors in the transport properties in the temperature range investigated are smaller than the experimental uncertainties. The dilute-gas and the excess terms together represent the so-called backgrounds $\bar{\eta}$ and $\bar{\lambda}$ of the viscosity and thermal conductivity, respectively [4]. The remaining contributions $\Delta_c \eta(\rho, T)$ and $\Delta_c \lambda(\rho, T)$ represent the critical enhancement of the viscosity and thermal conductivity, respectively. As the critical enhancement of the viscosity is small and occurs only in the very close vicinity of the critical point [12] and since for R152a no viscosity measurements exist in this region, the available experimental data for R152a can be represented by the background viscosity $\eta(\rho, T) = \bar{\eta}(\rho, T)$ = $\eta_0(T) + A_R \eta(\rho)$. However, the critical enhancement of the thermal conductivity is very significant. In order to separate the excess term and the critical enhancement term of the thermal conductivity, both contributions have to be determined in an iterative process as described in detail by Vesovic et al. [8].

To convert experimental pressures P into densities ρ and to calculate **the various thermodynamic properties needed for the evaluation of the critical enhancement contributions, we need an equation of state. For this purpose we have adapted a global equation of state developed by Tillner-Roth [7], far away from the critical point, and a crossover equation of state recently developed by van Pelt and Sengers [6], which incorporates the singular behavior of the thermodynamic properties near the critical point. Specifically, the equation of van Pelt and Sengers has been used in a range of temperatures T around the critical temperature bounded by [6]**

$$
365 \text{ K} \leq T \leq T_c \left(\frac{3}{4} + \frac{3\rho}{4\rho_c} - \frac{\rho^2}{3\rho_c^2} \right) \tag{3}
$$

where $T_c = 386.411$ K and $\rho_c = 368.0$ kg·m⁻³ are the critical temperature **and critical density, respectively. Outside this range the equation of state of Tillner-Roth has been used. Temperatures in this paper are in terms of ITS 90.**

Ref. No.	First author	P(MPa)	T(K)	Phase	Method	AME/MAX	Points
13	Assael	$1.5 - 18$	273-333		VW	$0.9/-2.6$	32
13	Assael		273-333	sl	VW	0.7/2.0	7
14	Mayinger	0.1	248-433	$\mathbf v$	OD	0.2/0.7	20
15	Takahashi	$0.1 - 5.3$	298-423	V	OD	$0.8/-2.1$	103
16	Takahashi	$0.1 - 0.7$	273-303	v	0D	$0.6/-1.8$	49
17	van der Gulik		243-373	sl	VW	0.9/2.4	35
18	Arnemann		243-352	sl	RB	3.4/10.1	12
19	Heide		233-333	sl	RB	$4.0/-7.0$	10
20	Kumagai		$273 - 343$	sl	C _V	1.8/6.3	8
21	Kumagai		$273 - 343$	sl	CV	2.7/9.0	8
22	Lapardin	$0.1 - 50$	156-434	l, v	CV	$7.3/-20$	47
14	Mayinger	$0.1 - 12$	253-493	$\mathbf v$	OD	2.1/20	209
14	Mayinger		249-386	sv	OD	5.9/34	12
23	Mears		243-333	sl	CV	40/63	8
24	Nagaoka	0.1	298-323	v	RB	0.7/1.7	$\overline{2}$
25	Phillips		200-318	sl	CV	5.7/11	6
26	Sagaidakova		$163 - 383$	sl	C	$1.2/-6.3$	15
27	Schramm		233-600	dil	С	$0.6/-0.9$	8
28	Takahashi		294-386	SV	OD.	$3.0/-5.9$	19
17	van der Gulik		243-373	sv	٧W	8.0/27	36

Table I. Viscosity References-Comparison with Eq. (1)^a

^{*a*} Phase: dil = dilute gas; $l =$ liquid; $v =$ vapor; $s =$ saturated. Method: $C =$ calculated; $CV =$ **capillary viscometer;** OD = **oscillating disk;** RB = rolling ball; VW = vibrating wire. AME/ MAX: **absolute mean error (%)/maximum error (%). Points: number of points compared within the range of validity of the correlation.**

3. BACKGROUND VISCOSITY

The viscosity of R152a has been measured mainly in the liquid region at saturation. Four pressure-dependent data sets are available in the vapor phase, and three at saturated-vapor states. No experimental data near the critical point have been reported. In Table I we list 16 references for the viscosity together with the total pressure and temperature ranges, the phase, the experimental method, and the deviation of each data set with respect to the present correlation. The references listed above the solid line were used for the correlation. The data analysis shows that more measurements are desirable, especially in the subcritical vapor phase and in the critical region.

3.1. Dilute-Gas Viscosity

The dilute-gas viscosity η_0 is represented by an expression derived from the kinetic theory of gases,

$$
\eta_0 = \frac{5}{16} \sqrt{\frac{MkT}{\pi N_A}} \frac{10^{24}}{\sigma^2 \Omega_\eta(T^*)} = \frac{0.2169614 \sqrt{T}}{\sigma^2 \Omega_\eta(T^*)}
$$
(4)

Fig. 1. The viscosity η_0 of R152a in the dilute-gas limit. The solid line represents the values calculated from Eq. (4); the data points shown are those reported by Takahashi et al. [15] (\Box), Takahashi et al. [16] (\triangle), and Mayinger [14] (\bigcirc).

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where $M=0.06605$ kg·mol⁻¹ is the molecular mass, k is Boltzmann's constant in $J \cdot K^{-1}$, N_A is Avogadro's number in mol⁻¹, and T is the temperature in K; η_0 obtained from this equation is in μ Pa. s. The collision integral is represented by an equation developed by Bich et al. [29],

$$
\ln \Omega_{\eta}(T^*) = \sum_{i=0}^{4} A_i (\ln T^*)^i
$$
 (5)

with the reduced dimensionless temperature $T^* = kT/\varepsilon$ and the coefficients A_i listed in Table II. The energy scaling factor $\varepsilon/k = 354.84$ K and the length scaling factor $\sigma = 0.46115$ nm were estimated by fitting Eq. (4) to the experimental data reported by Takahashi et al. [15, 16] and Mayinger [14]. Figure 1 shows the equation for the dilute-gas viscosity as a solid line together with the above-mentioned data, which are indicated by symbols in the temperature range 240 to 440 K. The deviations are within $\pm 1\%$ as shown in Fig. 2.

Fig. 2. Relative deviations (%) of the experimental viscosity data of Takahashi et al. [15] (\square), Takahashi et al. [16] (\triangle), and Mayinger [14] (\bigcirc) from the corresponding values calculated with Eq. (4) for $\eta_0(T)$.

	Α.	E,
0	0.4425728	
	-0.5138403	-0.0737927
2	0.1547566	0.517924
3	-0.02821844	-0.308875
4	0.001578286	0.108049
5		-0.408387
		2.91733

Table II. Coefficients in Eqs. (5) and (6)

3.2. Excess Viscosity

The dimensionless excess viscosity

$$
\frac{A_{\rm R}\eta}{H_{\rm c}} = \sum_{i=1}^{4} E_i \left(\frac{\rho}{\rho_{\rm c}}\right)^i + \frac{E_5}{\rho/\rho_{\rm c} - E_6} + \frac{E_5}{E_6} \tag{6}
$$

Fig. 3. The dimensionless excess contribution to the viscosity of R152a. The solid line represents the values calculated from Eq. (6); the data points shown are those reported by Takahashi et al. [15] (\Box), Assael et al. [13] (\triangle), and van der Gulik [17] (\bigcirc).

Fig. 4. Relative deviations (%) of the experimental viscosity data of Takahashi et al. [15] (D) , Assael et al. [13] (\triangle) , and van der Gulik [17] (O) from the values calculated with Eqs. (4) and (6) for the background viscosity $\bar{\eta}$.

is represented by a fourth-order polynomial with a hyperbolic term accounting for the steep increase in the viscosity at high densities, where the viscosity reduction factor $H_c = 51.12 \mu \text{Pa} \cdot \text{s}$ is a so-called pseudo-critical viscosity deduced from a dimensional analysis $[9, 30]$. The coefficients E_i in Eq. (6) are given in Table II. They were determined from a fit to the vapor-phase data of Takahashi et al. [15], revised saturated-liquid data of van der Gulik [17], and measurements of Assael et al. $[13]$ as shown in Fig. 3. The equation represents the experimental data within $\pm 3\%$ from 240 to 440 K at pressures; up to 20 MPa and densities up to 1050 kg \cdot m⁻³, as shown in Fig. 4.

4. BACKGROUND THERMAL CONDUCTIVITY

The available references for the thermal conductivity of R152a are listed in Table III. Most measurements were carried out in the liquid phase. Six data sets exist for the thermal conductivity at atmospheric pressure. The correlation is based on the data sets listed above the solid line. Additional measurements are needed mainly in the subcritical vapor phase, even at atmospheric pressure, and in the near and extended critical region.

Ref. No.	First author	P(MPa)	T(K)	Phase		Method AME/MAX	Points
31	Afshar		280-510	dil	HW	1.0/3.2	10
32	Assael	$0.5 - 22$	253-333	1	HW, T	0.8/1.5	37
32	Assael		253-333	sl	HW, T	0.6/1.1	5
33	Gurova	$0.8 - 18$	$212 - 294$	1	HW, T	$1.5/-2.8$	24
34	Hammerschmidt	0.1	$303 - 463$	v	PP	1.3/2.4	5
35	Kim	$2.1 - 20$	223-323	\mathbf{I}	HW, T	0.5/2.1	20
35	Kim.		$223 - 323$	sl	HW, T	1.1/2.6	$\overline{\bf{4}}$
36	Kraft		279-386	sl	DLS.	1.3/3.2	15
37	Kruppa	$0.5 - 11$	293-426	l, v, sl	DLS -	$1.5/-4.3$	27
38	Taxis-Reischl	$0.1 - 2.4$	277-400	v	HW, T	1.3/6.5	54
39	Tsvetkov	$7.7 - 8.6$	$190 - 300$	1	CC, T	2.2/2.8	6
40	Geller	$0.1 - 6.9$	305-433	\mathbf{I}, \mathbf{v}	HW, S	3.9/16	126
41	Grebenkov	$1.0 - 20$	294-341		cc	$3.2/-7.1$	78
42	Gross	$0.1 - 6.2$	$253 - 313$		HS	3.6/4.1	18
43	Gross	$0.1 - 6.2$	$253 - 363$	l, v, sl, sv	HW, T	3.5/26	111
19	Heide		$233 - 333$	sl	CC	4.6/5.5	10
44	Ibreighith		278-323	1	DLS	5.3/20	24
45	Kesselman		213-333	sl	HW, S	$1.3/-2.6$	10
36	Kraft		360-386	sv	DLS	3.1/4.2	6
46	Tauscher		$163 - 298$	sl	HW. T	3.4/3.6	$\overline{7}$
47	Vargaftik	$0.2 - 4$	$265 - 500$	l, v	$_{\rm CO}$	2.9/10.5	41
48	Yata	$1.4 - 31$	$265 - 343$	1	HW, T	$2.8/- 6.0$	20
49	Yin	0.1	279-349	\mathbf{v}	HW, T	$8.5/-11$	14

Table III. Thermal Conductivity References—Comparison with Eq. (2)^a

" Phase: dil = dilute gas; $l =$ liquid; $v =$ vapor; $s =$ saturated. Method: $CC =$ coaxial cylinder; $CO =$ compilation; DLS = dynamic light scattering; HS = hot strip; HW = hot wire (S = steady state; T = transient); PP = parallel plate. AME/MAX: absolute mean error $(\%)/$ maximum error (%). Points: number of points compared within the range of validity of the correlation.

4.1. Dilute-Gas Thermal Conductivity

The dilute-gas function for the thermal conductivity

$$
\lambda_0 = B_0 + B_1 T \tag{7}
$$

is represented by an empirical linear polynomial with λ_0 in mW · m⁻¹ · K⁻¹ and the temperature T in K $[2, 3]$. It is based on the data of Afshar and Saxena [31], Hammerschmidt [34], and Taxis-Reischl [38] as indicated in Fig. 5 in the temperature range 280 to 460 K, but extrapolation down to 240 K seems possible. The coefficients B_i , in Eq. (7) are given in Table IV. Figure 6 shows that the uncertainty of the fit is about $\pm 3\%$.

	В.	L.
0	-14.9420	
	0.0973283	9.18090
$\mathfrak z$		11.8577
3		-5.44730
		1.71379

Table IV. Coefficients in Eqs. (7) and (8)

4.2. Excess Thermal Conductivity

The dimensionless excess thermal conductivity is expressed as

$$
\frac{\Delta_{\mathbf{R}}\lambda}{\Lambda_{\mathbf{c}}} = \sum_{i=1}^{4} L_i \left(\frac{\rho}{\rho_{\mathbf{c}}}\right)^i \tag{8}
$$

with the thermal-conductivity reduction factor $A_c = 1.155$ mW \cdot m⁻¹ \cdot K⁻¹ deduced from a dimensional analysis [9, 30]. The coefficients L_i are listed in Table IV. The correlation of the excess data is based on the measurements

Fig. 5. The thermal conductivity λ_0 of R152a in the dilute-gas limit. The solid line represents the values calculated from Eq. (7); the data points shown are those reported by Afshar and Saxena [31] (\Box), Hammerschmidt [34] (\triangle), and Taxis-Reischl $[38]$ (\bigcirc).

Fig. 6. Relative deviations (%) of the experimental thermal-conductivity data of Afshar and Saxena [31] (\Box), Hammerschmidt [34] (\triangle), and Taxis-Reischl [38] (O) from the values calculated with Eq. (7) for $\lambda_0(T)$.

of Assael et al. [32], Gurova et al. [33], Kim et al. [35], and Tsvetkov et al. [39] in the liquid phase, the vapor-phase measurements of Taxis-Reischl [38], and the thermal-diffusivity measurements of Kruppa and Straub [37] as well as those of Kraft and Leipertz [36], as shown in Fig. 7. Equation (8) is valid in the temperature range 240 to 440 K, at pressures up to 20 MPa and densities up to $1050 \text{ kg} \cdot \text{m}^{-3}$. The deviation plot in Fig. 8 shows that the equation represents the thermal-conductivity data within \pm 5% in both **the vapor and the liquid phase.**

5. THE CRITICAL REGION

In Section 2, each of the transport properties was decomposed into three terms; the first two determine the background contributions $\tilde{\eta}$ and $\overline{\lambda}$, while $A_c\eta$ and $A_c\lambda$ represent the increase in the transport properties due to **critical fluctuations. The critical enhancements are represented by a theoretical crossover model originally developed by Olchowy and Sengers [12], which has been used previously to represent the transport properties of a variety of fluids in the critical region [8-11, 30,50-55] and which recently has been slightly modified by Luettmer-Strathmann et al. [56, 57]**

Fig. 7. The dimensionless excess contribution to the thermal conductivity of RI52a. The solid line represents the values calculated from Eq.(8); the data points shown are those reported by Taxis-Reischl [38] (\Box), Kim et al. [35] (\triangle), Assael et al. [32] (∇), Tsvetkov et al. [39] (\diamond), Gurova et al. [33] (\odot), Kruppa and Straub [37] (\bullet), and Kraft and Leipertz $[36]$ (\times).

This crossover model is based on the mode-coupling theory for the dynamical behavior of critical fluctuations [56].

The thermal diffusivity D_T is related to the thermal conductivity λ as

$$
D_{\rm T} = \frac{\lambda}{\rho c_{\rm p}}\tag{9}
$$

where c_p is the isobaric specific heat capacity. The critical part A_cD_T of the thermal diffusivity is given by

$$
\Delta_c D_T = \frac{\Delta_c \lambda}{\rho c_p} \tag{10}
$$

Fig. 8. Relative deviations (%) of the experimental thermal-conductivity data of Taxis-Reischl [38] (\Box), Kim et al. [35] (\triangle), Assael et al. [32] (\triangledown), Tsvetkov et al. [38] (\diamond), Gurova et al. [33] (\bigcirc), Kruppa and Straub [37] (\bullet), and Kraft and Leipertz [36] (\times) from the values calculated with Eqs. (7) and (8) for the background thermal conductivity $\bar{\lambda}$.

Asymptotically close to the critical point $\Delta_c D_T$ satisfies a Stokes-Einstein relation of the form [4]

$$
\Delta_{\rm c} D_{\rm T} = \frac{R_0 kT}{6\pi\eta\xi} \tag{11}
$$

where k is Boltzmann's constant, ξ the correlation length of the critical fluctuations, and R_0 a universal amplitude for which we adopted a value of $R_0 = 1.03$ [9].

The viscosity exhibits a weak divergent critical enhancement of the form [4]

$$
\Delta_c \eta = \bar{\eta} \left[(Q\xi)^z - 1 \right] \tag{12}
$$

where Q is a system-dependent amplitude and where $z = 0.063$ is a universal critical exponent [58-60].

In the crossover model these asymptotic expressions are generalized to

$$
\Delta_{\rm c} D_{\rm T} = \frac{R_0 kT}{6\pi\eta\xi} \left(\Omega - \Omega_0\right) \tag{13}
$$

$$
\eta = \bar{\eta} e^{czH} \tag{14}
$$

where $\Omega - \Omega_0$ and H are crossover functions that depend on the thermodynamic properties, on the correlation length ξ , and on the background transport properties $\bar{\lambda}$ and $\bar{\eta}$ and they contain one system-dependent parameter q_{D} , which represents a cutoff wavenumber of the critical fluctuations [50]. The coefficient c in expression (14) for η is given by [55].

$$
c = \left(2 - \frac{\alpha + \gamma}{2\nu}\right)^{-1} = 1.075\tag{15}
$$

where $\alpha = 0.110$, $\gamma = 1.239$, and $\nu = 0.630$ are the critical exponents for the isochoric specific heat capacity c_v , the susceptibility $\chi = \rho(\partial \rho/\partial p)_T$, and the correlation length ξ , respectively [58]. Detailed expressions for the crossover functions Ω , Ω_0 , and H have been presented in previous publications [50, 53]. For the present correlation we have used similar but slightly modified expressions as specified elsewhere [56, 57].

The crossover functions depend on the correlation length ξ , which for practical purposes is calculated from the dimensionless susceptibility

$$
\chi^*(T,\rho) = \frac{\rho P_c}{\rho_c^2} \left(\frac{\partial \rho}{\partial P}\right)_T
$$
 (16)

where $P_c = 4.520 \text{ MPa}$ is the critical pressure, through an equation of the form [9]

$$
\xi = \xi_0 \left[\frac{1}{\Gamma} \left(\chi^*(T, \rho) - \chi^*(T_{\text{ref}}, \rho) \frac{T_{\text{ref}}}{T} \right) \right]^{\nu/\gamma} \tag{17}
$$

Here $\xi_0 = 1.894 \times 10^{-10}$ m and $\Gamma = 0.0487$ are the amplitudes of the critical power laws for ζ and χ^* [58] and whose values can be deduced from the asymptotic behavior of the equation of state [6]. T_{ref} is a reference temperature which is chosen in such a way that the critical enhancement of the thermal conductivity $\mathcal{A}_{c}\lambda$ is negligibly small for temperatures greater than T_{ref} ; we continued to choose $T_{ref} = \frac{3}{2}T_c$ as previously adapted for R134a [9]. The cutoff wavenumber q_D was treated as an adjustable constant to be determined from a fit to experimental thermal-diffusivity data [37]. The values of all constants that appear in the equations (13) for

TableV. Constants in the Equations for the Critical Enhancements $\Delta_c \eta$ and $\Delta_c \lambda$

```
Critical parameters 
     T_c = 386.411 \text{ K}\rho_c = 368.0 \text{ kg} \cdot \text{m}^{-3}P_c = 4.520 MPa
 Universal constants 
        R_0 = 1.03z = 0.063y = 1.239v = 0.63\alpha = 0.110Critical amplitudes 
        \Gamma = 0.0487\xi_0 = 1.894 \times 10^{-10} m
Reference temperature 
        T_{\text{ref}} = \frac{3}{2} T_{c}Cutoff wavenumber 
q_{\rm D}^{-1} = 4.37 × 10<sup>-10</sup> m
```
 A_cD_T and (14) for $\eta/\bar{\eta}$ are listed in Table V. The critical enhancement $A_c\lambda$ of the thermal conductivity is deduced from $A_r D_T$ through Eq. (10). The various thermodynamic properties in the crossover model were calculated from the equations of state of van Pelt and Sengers [6] and of Tillner-Roth [7] as specified in Section 2.

Thermal-diffusivity data deduced from dynamic light-scattering measurements have been obtained by Kraft and Leipertz [36] and by Kruppa and Straub [37] for R152a in the critical region. Kruppa and Straub obtained 300 data points along seven isotherms on the liquid and vapor sides of the phase boundary, as well as along the critical isochore. Kraft and Leipertz have reported 22 data points along the liquid and vapor sides of the phase boundary.

Kruppa and Straub found a critical temperature of $T_c = 386.442$ K (ITS90) from their data. Since we used a value of $T_c = 386.411 \text{ K}$ [6], we shifted their temperatures by -0.031 K. Furthermore, they quote a critical density of $\rho_c = 368 \text{ kg} \cdot \text{m}^{-3}$ taken from the literature [62] for their calculations, but the thermal-diffusivity data for the lowest supercritical isotherm show that p_c might be slightly larger. Therefore, we adopted a value of $\rho_c = 369.5 \text{ kg} \cdot \text{m}^{-3}$ for their data and recalculated their densities according to this assumption.

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In the absence of actual measurements of the thermal conductivity λ in the critical region, we instead calculated λ from the experimental thermal diffusivity D_T as

$$
\lambda = \rho c_p D_T \tag{18}
$$

The uncertainty in the thermal conductivity data obtained according to the above equation can be calculated in the following way: Kruppa and Straub claim uncertainties of 0.5 to 5 % in their thermal-diffusivity values, of less than 20 mK in their temperatures, and of about 0.3 % in the densities. The specific-heat values used were calculated from the fundamental equation of state, which consists of the crossover model of van Pelt and Sengers [6] and the Tillner-Roth equation [7]. Since van Pelt and Sengers do not give the uncertainties in this quantity explicitly, but show a plot of regions where the deviation in c_p from the corresponding point calculated from the

Fig. 9. The thermal conductivity of RI52a in the critical region as a function of density. The symbols indicate values calculated from the experimental thermaldiffusivity data of Kruppa and Straub [37] along the various isotherms: $(*)$ 367 K; (x) 382 K; (\bigcirc) 386 K; (\bigcirc) 387 K; (\Box) 390 K; (\triangle) 405 K; (\Diamond) 425 K. The solid curves represent the respective values calculated from all three terms in the representative Eq. (2) in this paper.

Fig. 10. The thermal diffusivity of R152a in the critical region as a function of density. The symbols indicate thermal-diffusivity data measured by Kruppa and Straub [37] along one of the respective isotherms: (*) 367 K; (\times) 382 K; (\circlearrowright) 386 K; (\bullet) 387 K; ($+$) 390 K; (\circlearrowright) 405 K; (\bullet) 425 K. The solid curves represent the corresponding values calculated from Eqs. (2) and (19).

Tillner-Roth equation alone is less than 0.1, 0.5, and 1%, respectively, we estimate an error of 2% in the region where we apply this equation. (Tillner-Roth himself quotes an uncertainty of 2% in c_p for his equation of state [7].) Combined with the errors Kruppa and Straub quoted for the temperature and density, the total uncertainty in the c_P values, which were used to convert the D_T data into thermal conductivities, ranges from 2% away from the critical point to about 7% near the critical point on the lowest temperature supercritical isotherm (386.83 K) . Adopting the value of 2% for the uncertainty in D_T and 0.3% for that in the density, the estimated uncertainties in λ are slightly higher, ranging from 2.8 to 7%.

The cutoff wavenumber q_D , the only adjustable constant in the expression for $\Delta_c D_T$, was determined from a least-squares fit of the values for λ thus deduced from the measurements of Kruppa and Straub to

$$
\lambda = \bar{\lambda} + \Delta_c \lambda = \lambda_0(T) + \Delta_R \lambda(\rho) + \rho c_P \Delta_c D_T \tag{19}
$$

where $\lambda_0(T)$ and $\Delta_R \lambda(\rho)$ are the background contributions introduced in Eq. (2) (Section 2) and where A_cD_T is given by Eq. (13). For the fitting procedure all the data in the one-phase region taken along the seven isotherms except for those with densities greater than 600 kg \cdot m⁻³ and two data points of the 386.06 K isotherm closest to the phase boundary were used. In this way data that are suspected of having larger errors due to lower light-scattering intensities are excluded from the fit. Thus we found a value of $q_D^{-1} = 4.37$ Å, somewhat larger than reported for other fluids $[8-11, 30, 50-55]$. The values of all constants in the equations for the critical enhancements of the transport properties are given in Table V.

In Fig. 9, the thermal-conductivity data calculated from the thermaldiffusivity data of Kruppa and Straub as well as the values calculated from the crossover theory are displayed graphically. The absolute mean error (AME) for the complete set of Kruppa and Straub is about 3%, the maximum error being \pm 14%. In Figs. 10 and 11, comparisons between their thermal-diffusivity data along the seven isotherms, the phase boundary,

Fig. 11. The thermal diffusivity of R152a on the critical isochore and on the phase boundary as fimctions of the reduced temperature. The symbols indicate experimental values obtained by Kruppa and Straub [37]: (*) critical isochore: (\bigcirc) liquid phase: (\times) vapor phase. The solid curves represent the corresponding values calculated from the crossover model for transport properties.

Fig. 12. The thermal difusivity of R152a along the phase boundary. The symbols indicate the thermal diffusivity data measured by Leipertz and Kraft [36]: (O) liquid phase; (\times) vapor phase. The solid lines represent values calculated from the crossover model for transport properties.

and along the critical isochore, respectively, are shown. The agreement between theoretical and experimental data is satisfactory. The experimental thermal-diffusivity data measured by Kraft and Leipertz along the phase boundary are plotted together with the corresponding theoretical values in Fig. 12. After having shifted their temperatures by $+0.23$ K, which seems justifiable since they do not quote a value for T_c along with their data, the agreement is quite good.

As mentioned in Section 3, no data are available for the viscosity in the critical region.

6. RESULTS

The viscosity η can be calculated from Eq. (1), where the dilute-gas term $\eta_0(T)$ is represented by Eq. (4) and where the equation for the excess contribution $\Delta_R \eta(\rho)$ is given by Eq. (6). The critical enhancement $\Delta_c \eta$ can be estimated from Eq. (14). The thermal conductivity λ can be calculated from Eq. (2), where the dilute-gas term $\lambda_0(T)$ is represented by Eq. (7), the equation for the excess contribution $\Delta_R \lambda(\rho)$ is given by Eq. (8), while the critical enhancement $\Delta_c \lambda$ can be calculated from Eqs. (13) and (10). The correlating equations for both transport properties are valid for temperatures ranging from 240 to 440 K, for pressures up to 20 MPa, and for densities up to $1050 \text{ kg} \cdot \text{m}^{-3}$.

Values for the viscosity and the thermal conductivity of R152a, as calculated from Eqs. (1) and (2) are listed in Tables VI, VII, and VIII. Specifically, Table VI gives the transport properties at saturation as a function of temperature, where a single prime refers to the saturated liquid and a double prime to the saturated vapor. Values calculated for the transport properties at $P = 0.1$ MPa, indicated by the subscript 0.1, are also presented in Table VI. Values calculated for the transport properties at selected temperatures and pressures are listed in Tables VII and VIII.

The region where the critical enhancement of the viscosity exceeds 1% of the total viscosity can be approximated by a trapezoid with the corners

Similarly the region where the critical enhancement of the thermal conductivity $\Delta_{\alpha} \lambda$ exceeds 3% of the total quantity λ is bounded approximately by

Actually, a critical-enhancement contribution to the thermal conductivity extends to higher temperatures beyond 440 K, but 440 K is the maximum temperature of validity of the present correlation.

The overall uncertainty in the background correlation for the viscosity is estimated as $\pm 3\%$; that for the thermal conductivity, as $\pm 5\%$.

7. CONCLUSION

Based on a critical review of the available data, equations for the viscosity and thermal conductivity of R152a were developed that are valid in a wide range of temperatures and pressures, including the critical region. Analysis and evaluation of the experimental data showed that, for the viscosity, further precise measurements are needed, especially in the subcritical vapor phase and in the near and extended critical region. In the

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Table VI. (Continued)

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case of the thermal conductivity of R152a we also need more precise measurements in the subcritical vapor phase, even at atmospheric pressure, as well as in the near and extended critical region.

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